## UC Berkeley Math 10B, Spring 2015: Midterm 1

Prof. Sturmfels, February 26, 2015

| Name:      |      |   |              |                     |         |          |  |
|------------|------|---|--------------|---------------------|---------|----------|--|
| SID:       |      |   |              |                     |         |          |  |
| Neighbors: |      | Please write the names of the students next to you (or "None"): |              |                     |         |          |  |
| L          | eft: |   |              |                     |         |          |  |
| Rig        | ght: |   |              |                     |         |          |  |
| Section:   |      | Circle your discussion section below:                           |              |                     | Grading | Grading  |  |
|            | Sec  | Time  | Room         | GSI                 | 1       | / 5      |  |
|            | 101  | MWF 8-9   | 121 Latimer  | Jason Ferguson      | 2       | / 5      |  |
|            | 102  | MWF 9-10  | 104 Barrows  | Jason Ferguson      | ŋ       | ,<br>/ E |  |
|            | 103  | MWF 10-11   | 237 Cory     | Minseon Shin        | 3       | / 5      |  |
|            | 104  | MWF 11-12   | 121 Latimer  | Indraneel Kasmalkar | 4       | / 5      |  |
|            | 105  | MWF 12-1  | 237 Cory     | Indraneel Kasmalkar | ۳       | ·<br>/ F |  |
|            | 106  | MWF 1-2   | 206 Wheeler  | Joe Kileel          | 5       | / 5      |  |
|            | 107  | MWF 2-3   | 283 Dwinelle | Joe Kileel          | 6       | / 5      |  |
|            | 108  | MWF 9-10  | 110 Wheeler  | Minseon Shin        | 7       | ·<br>/ F |  |
|            | 109  | MWF 1-2   | 250 Dwinelle | Elina Robeva        | (       | / 5      |  |
|            | 110  | MWF 2-3   | 228 Dwinelle | Elina Robeva        | 8       | / 5      |  |
|            | Othe | or/none evolai  | n•           |                     |         | /40      |  |

## **Instructions:**

• Closed book: No notes, no books, no calculators.

Other/none, explain:

- The exam time is 80 minutes. Do all 8 problems.
- You must justify your answers for full credit.
- Write your answers in the space below each problem.
- Answers in complete sentences are encouraged.
- If you need more space, use reverse side or scratch pages. Indicate clearly where to find your answers.

**1.** (5 points) Find the coefficient of  $x^6y^4$  in  $\left(2x + \frac{1}{2}y\right)^{10}$ .

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| 3. | (5 points) Seven people stand in line to greet the President of the United States. However, one of the seven people is nervous and does not want to be the first person in line. In how many different ways can the seven people stand? |
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| 4. | (5 points) An unbiased coin is tossed 5 times. number of times you will see an $H$ immediately | What is the expected value of th followed by a $T$ ? |
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5. (5 points) How many ways are there to divide 5 people into 2 or 3 groups?

(The order of the groups and the order of the people in each group do not matter. In your answer, you must state the actual number, which is a positive integer.)

**6.** (5 points) Box A contains 1 white ball and 4 black balls. Box B contains 1 white ball and 3 black balls. We flip a fair coin. If the outcome is heads, then a ball from box A is selected at random. If the outcome is tails, then a ball from box B is selected at random. Suppose that a white ball is selected. What is the probability that the coin landed tails?

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- **8.** (5 points) Let X be the most number of heads you get in a row after flipping a fair coin five times. For example, if you got "HHHHHH" then X=3; if you got "HTTHT" then X=1; and if you got "TTTTT" then X=0.
  - (a) Explain why X is a random variable by showing it fits your definition in 7.

(b) Explain why " $X \ge 2$ " is an event by showing it fits your definition in 7.

(Scratch Paper, Page 1)

(Scratch Paper, Page 2)

(Scratch Paper, Page 3)